

Discussion 7

BCS74)  $v_i$  weakly dominates lower bids because bidding lower only affects probability of winning, not amount paid.  
 -  $v_i$  does not weakly dominate higher bid because, for example, you would want to bid high if:

- $v_n < v_i < v_j$
- Bid valuation not Nash because bidder 2 deviates.
- Symmetric Nash at  $b_i = v_i$ .

BCS75) Single-object yield revenue  $16 + 10 + 12 = 38$   
 Bundled-object yield revenue  $16 + 28 = 44$

3) 2 player, either buy stocks or crypto. Stocks are safe and yield  $r$ . Crypto only increases in value if other buys.  
 ↳ Both buy yields  $m > r$ .  
 ↳ One buy yields 0.

First mixed Nash.

|                         |        |        |        |       |
|-------------------------|--------|--------|--------|-------|
|                         |        | Stock  | Crypto |       |
| Player 1<br>Nash yields | Stock  | $r, r$ | $r, 0$ | (q)   |
|                         | Crypto | $0, r$ | $m, m$ | (1-q) |
|                         |        | (q)    | (1-q)  |       |

↳ P1 stock:  $qr + (1-q)r = q \cdot 0 + (1-q)m$  ∴ P1 crypto.  
 $r = (1-q)m$   
 $1 - \frac{r}{m} = q$

↳ P2 symmetric.

Equilibrium:  $((1 - \frac{r}{m}, \frac{r}{m}), (1 - \frac{r}{m}, \frac{r}{m}))$ .

4.) There are 22 index cards. P1 can remove either 1 or 2, then P2 remove either 1 or 2, so on. Winner removes last card. Who has winning strategy?

↳ 3 stars left (other player move) is winning scenario.

↳ So is 6, 7, 12, 15, 18, 21.

↳ So P1 has winning strategy (must remove 1 first).

midterm)

$V_1$

$V_2$

2a) (up down)

b) Both do.

c)  $b > c$

d)  $s < c$

3a) 360, 370, 360, 370, yes

b) 440, 470, 470, 500, yes

c) No

4a)  $q_i = \frac{120 - q_i}{3}$

b) (30, 30)

c) 1350

d) 2400

same as  $V_1$

$q_i = \frac{100 - q_i}{5}$

(16.7, 16.7)

694.4

1000